

## Arithmetic Sequences

Determine if the sequence is arithmetic. If it is, find the common difference.

1) 35, 32, 29, 26, ...  
 $d = -3$

2) -3, -23, -43, -63, ...  
 $d = -20$

3) -34, -64, -94, -124, ...  
 $d = -30$

4) -30, -40, -50, -60, ...  
 $d = -10$

5) -7, -9, -11, -13, ...  
 $d = -2$

6) 9, 14, 19, 24, ...  
 $d = 5$

Given the explicit formula for an arithmetic sequence find the first five terms and the term named in the problem.

7)  $a_n = -11 + 7n$

Find  $a_{34}$ 

-4, 3, 10, 17, 24

$a_{34} = -4 + 7(33) = 227$

8)  $a_n = 65 - 100n$

Find  $a_{39}$ 

-355, -1355, -2355, -3355, -4355

$a_{39} = -3835$

9)  $a_n = -7.1 - 2.1n$

Find  $a_{27}$ 

-9.2, -11.3, -13.4, -15.5, -17.6

$a_{27} = -63.8$

10)  $a_n = \frac{11}{8} + \frac{1}{2}n$

Find  $a_{23}$ 

$\frac{15}{8}, \frac{19}{8}, \frac{23}{8}, \frac{27}{8}, \frac{31}{8}$        $a_{23} = \frac{103}{8}$

Given the first term and the common difference of an arithmetic sequence find the first five terms and the explicit formula.

11)  $a_1 = 28, d = 10$

12)  $a_1 = -38, d = -100$

28, 38, 48, 58, 68

-38, -138, -238, -338, -438

$a_n = 18 + 10n$  or  $a_n = 28 + 10(n-1)$

$a_n = 62 + 100n$

13)  $a_1 = -34, d = -10$

14)  $a_1 = 35, d = 4$

-34, -44, -54, -64, -74

35, 39, 43, 47, 51

$a_n = -24 - 10n$

$a_n = 31 + 6n$

Given a term in an arithmetic sequence and the common difference find the first five terms and the explicit formula.

15)  $a_{38} = -53.2, d = -1.1$

$$a_1 - (1.1)(37) = -53.2$$

$$a_1 = -11.4 \quad -12.5, -13.6, -14.7, -15.8$$

$$a_n = -11.4 - 1.1n$$

17)  $a_{37} = 249, d = 8$

$$a_1 + 8(36) = 249$$

$$a_1 = -47$$

$$a_n = -47 + 8n$$

16)  $a_{40} = -1191, d = -30$

$$a_1 - 30(39) = -1191$$

$$a_1 = 9$$

$$-21, -51, -81, -111, -141$$

$$a_n = 9 - 30n$$

18)  $a_{36} = -276, d = -7$

$$a_1 - 7(35) = -276$$

$$a_1 = -24$$

$$a_n = -24 - 7n$$

Given the first term and the common difference of an arithmetic sequence find the recursive formula and the three terms in the sequence after the last one given.

19)  $a_1 = \frac{3}{5}, d = -\frac{1}{3}$

$$\begin{cases} a_1 = \frac{3}{5} \\ a_n = a_{n-1} - \frac{1}{3} \end{cases}$$

21)  $a_1 = -26, d = 200$

$$\begin{cases} a_1 = -26 \\ a_n = a_{n-1} + 200 \end{cases}$$

20)  $a_1 = 39, d = -5$

$$\begin{cases} a_1 = 39 \\ a_n = a_{n-1} - 5 \end{cases}$$

$$34, 29, 24$$

22)  $a_1 = -9.2, d = 0.9$

$$\begin{cases} a_1 = -9.2 \\ a_n = a_{n-1} + 0.9 \end{cases}$$

Given a term in an arithmetic sequence and the common difference find the recursive formula and the three terms in the sequence after the last one given.

23)  $a_{21} = -1.4, d = 0.6$

$$a_1 + 20(0.6) = -1.4$$

$$\begin{cases} a_1 = -13.4 \\ a_n = a_{n-1} + .6 \end{cases}$$

25)  $a_{18} = 27.4, d = 1.1$

$$a_1 + 17(1.1) = 27.4$$

$$\begin{cases} a_1 = 8.7 \\ a_n = a_{n-1} + 1.1 \end{cases}$$

24)  $a_{22} = -44, d = -2$

$$a_1 - 21(-2) = -44$$

$$\begin{cases} a_1 = -2 \\ a_n = a_{n-1} - 2 \end{cases}$$

26)  $a_{12} = 28.6, d = 1.8$

$$a_1 + 11(1.8) = 28.6$$

$$\begin{cases} a_1 = 8.8 \\ a_n = a_{n-1} + 1.8 \end{cases}$$

Given two terms in an arithmetic sequence find the recursive formula.

27)  $a_{18} = 3362$  and  $a_{38} = 7362$

$$d = \frac{7362 - 3362}{38 - 18} = 200$$

$$\begin{cases} a_1 = -38 \\ a_n = a_{n-1} + 200 \end{cases}$$

28)  $a_{18} = 44.3$  and  $a_{33} = 84.8$

$$d = \frac{84.8 - 44.3}{33 - 18} \approx 2.7$$

$$\begin{cases} a_1 = -1.6 \\ a_n = a_{n-1} + 2.7 \end{cases}$$